

# EE 330

## Lecture 15

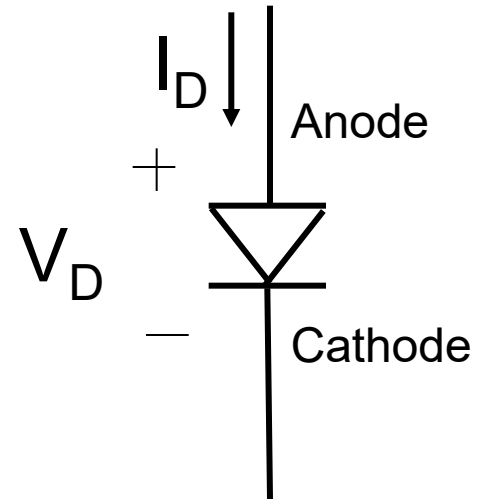
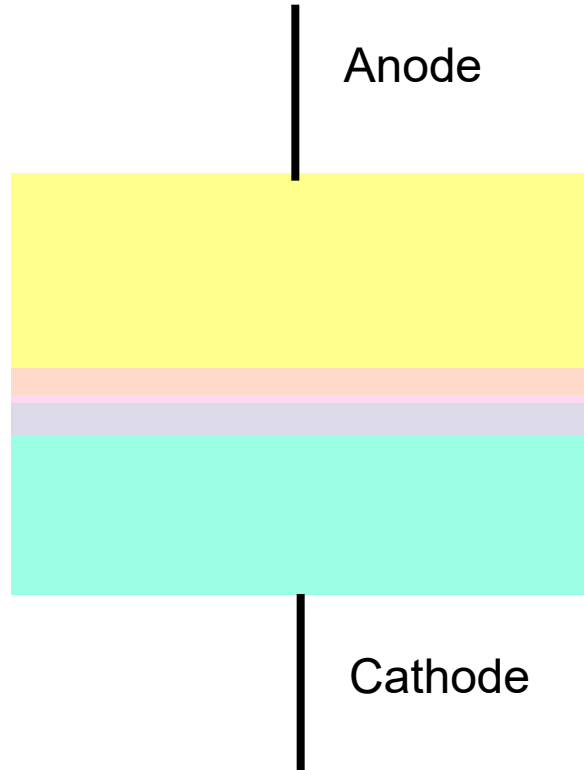
### Devices in Semiconductor Processes

- Diodes
- Analysis of Nonlinear Circuits

# Fall 2024 Exam Schedule

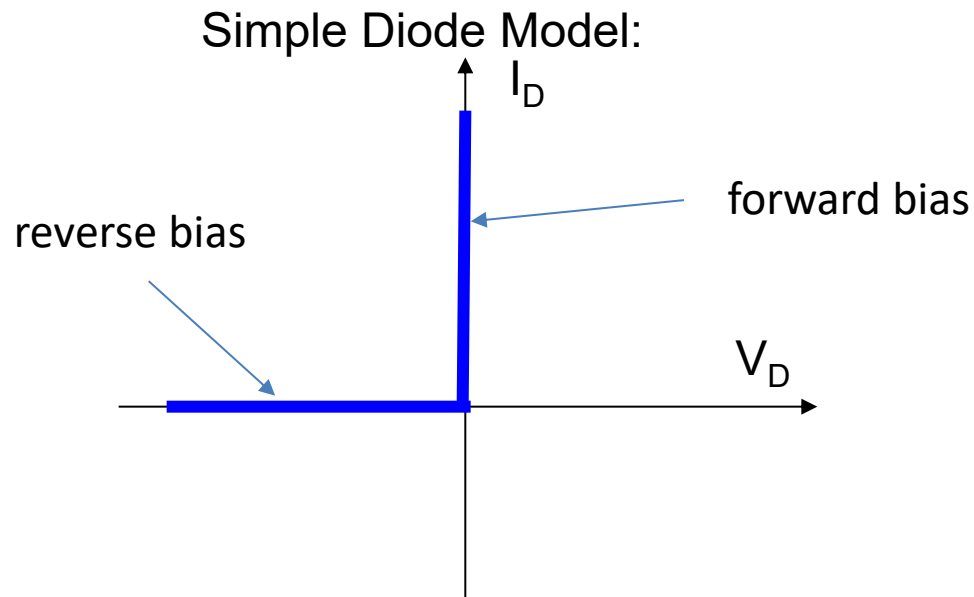
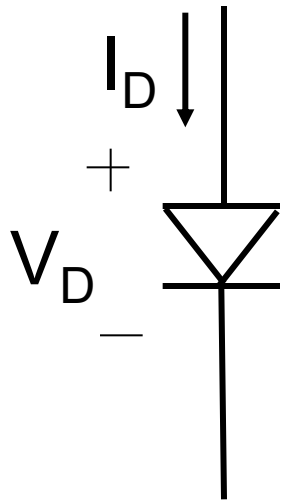
Exam 1	Friday	Sept 27
Exam 2	Friday	October 25
Exam 3	Friday	Nov 22
Final Exam	Monday	Dec 16 12:00 - 2:00 PM

# pn Junctions



Circuit Symbol

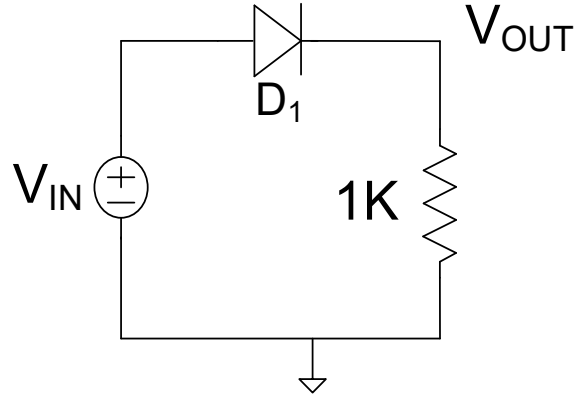
# pn Junctions



- This is a piecewise model
- pn junction serves as a “rectifier” passing current in one direction and blocking it in the other direction

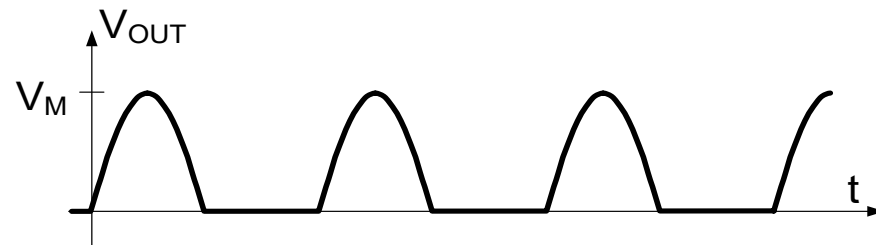
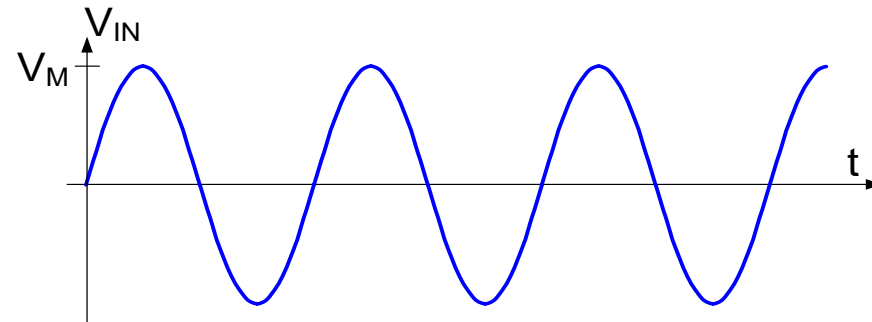
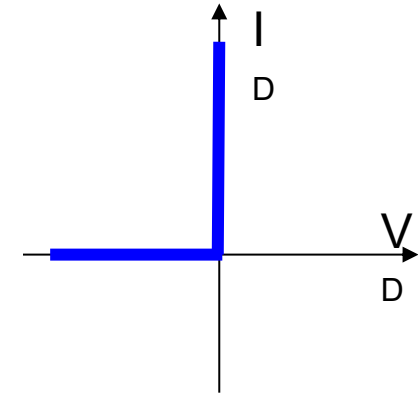
Review from last lecture

# Rectifier Application:



$$V_{IN} = V_M \sin \omega t$$

Simple Diode Model:

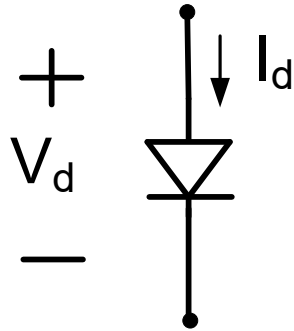


Analysis based upon “passing current” in one direction and “blocking current” in the other direction

# I-V characteristics of pn junction

(signal or rectifier diode)

Improved Diode Model:



Diode Equation

$$I_D = I_S \left( e^{\frac{V_d}{nV_t}} - 1 \right)$$

$I_S$  and  $n$  are model parameters

What is  $V_t$  at room temp?

$V_t$  is about 26mV at room temp

$I_S$  in the 10fA to 100fA range

$I_S$  proportional to junction area

$$V_t = \frac{kT}{q}$$

$$k = 1.380\,64852 \times 10^{-23} \text{ JK}^{-1}$$

$$q = -1.60217662 \times 10^{-19} \text{ C}$$

$$k/q = 8.62 \times 10^{-5} \text{ VK}^{-1}$$

$n$  typically about 1

Diode equation due to William Shockley, inventor of BJT

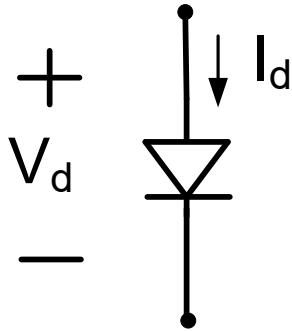
In 1919, [William Henry Eccles](#) coined the term **diode**

In 1940, Russell Ohl “stumbled upon” the p-n junction diode

# I-V characteristics of pn junction

(signal or rectifier diode)

Improved Diode Model:

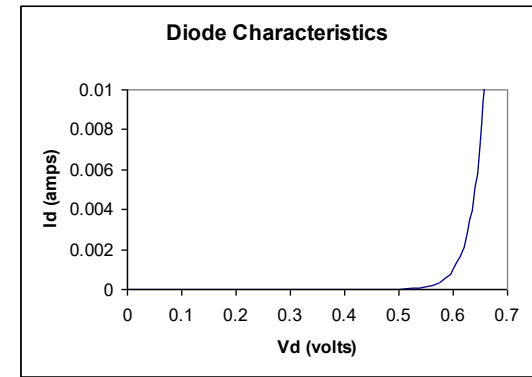


**Diode Equation**  $I_D = I_S \left( e^{\frac{V_d}{nV_t}} - 1 \right)$   
(not a piecewise model !)

**Simplification of Diode Equation:**

Under reverse bias ( $V_d < 0$ ),  $I_D \cong -I_S$

Under forward bias ( $V_d > 0$ ),  $I_D = I_S e^{\frac{V_d}{nV_t}}$



$I_S$  in 10fA -100fA range (for signal diodes)

$n$  typically about 1

$$V_t = \frac{kT}{q}$$

$$k/q = 8.62 \times 10^{-5} \text{ VK}^{-1}$$

$V_t$  is about 26mV at room temp

Simplification essentially identical model except for  $V_d$  very close to 0

Diode Equation or forward bias simplification are unwieldy to work with analytically

# pn Junctions

Diode Equation: (simplification)  $I = \begin{cases} I_S A e^{\frac{V}{nV_T}} & V > 0 \\ -I_S & V < 0 \end{cases}$  forward bias reverse bias

Diode Equation: (further simplification)  $I = \begin{cases} I_S e^{\frac{V}{nV_T}} & V > 0 \\ 0 & V < 0 \end{cases}$  forward bias reverse bias

$$I_S = J_S A$$

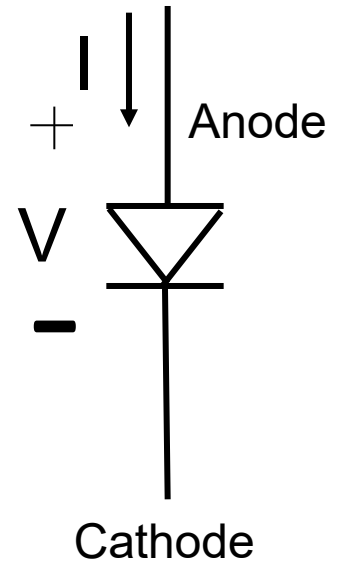
{ $J_S$ } is model parameter (or  $I_S$  is a model parameter if  $A$  is fixed)

{ $A$ } is design parameter,  $A$  is the cross-sectional area of the junction (usually from top view in layout)

Slight discontinuity at  $V=0$  in these models (which doesn't exist in real diodes) but of no consequence unless  $V$  is very close to 0

$I_S$  is often given in data sheets and model files

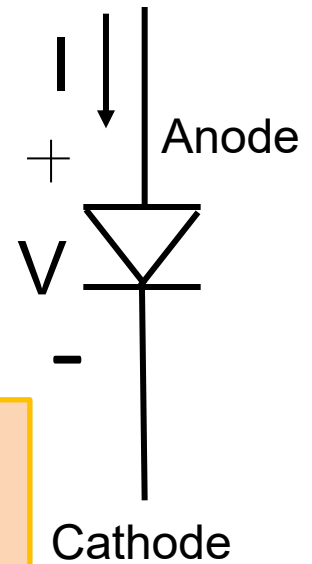
These are termed “piecewise” models





# Diode Model Summary

Ideal Diode Model	$V_D = 0$	$I_D > 0$	forward bias
	$I_D = 0$	$V_D < 0$	reverse bias



$$I_S = J_S A$$

Diode Equation

$$I_D = I_S \left( e^{\frac{V_d}{nV_t}} - 1 \right)$$

Diode Equation: (simplification)

$$I = \begin{cases} I_S e^{\frac{V}{nV_T}} & V > 0 \\ -I_S & V < 0 \end{cases}$$

forward bias  
reverse bias

Diode Equation: (further simplification)

$$I = \begin{cases} I_S e^{\frac{V}{nV_T}} & V > 0 \\ 0 & V < 0 \end{cases}$$

forward bias  
reverse bias

Little difference in these models, if any, in most applications. Typically, any referred to as the Diode Equation

# pn Junctions

**Diode Equation:** (further simplification)

$$I = \begin{cases} J_s A e^{\frac{V}{nV_T}} & V > 0 \quad \text{forward bias} \\ 0 & V < 0 \quad \text{reverse bias} \end{cases}$$

$$I_s = J_s A$$

$J_s$  (or  $I_s$ ) is strongly temperature dependent

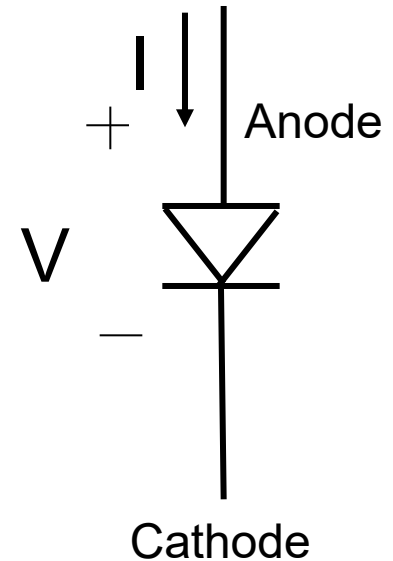
With  $n=1$ , for  $V>0$ ,

$$J_s = J_{sX} T^m e^{\frac{-V_{G0}}{V_t}}$$

$\{J_{sX}, m, n\}$  are model parameters

$\{A\}$  is a design parameter

$\{T, V_{G0}, k/q\}$  are environmental parameters and physical constants



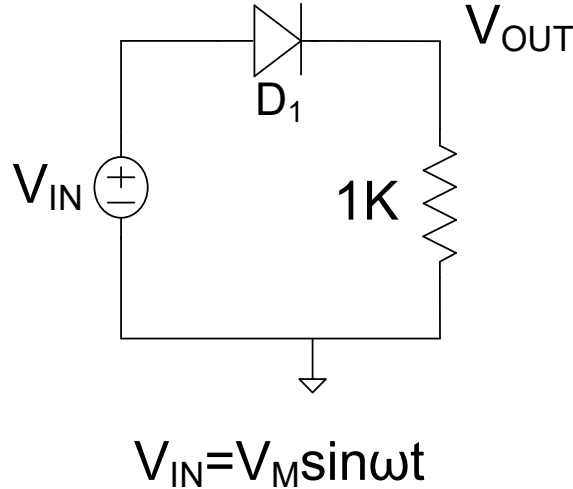
**Diode Equation:** (further simplification showing more detail)

$$I(T) = \begin{cases} \left( J_{sX} \left[ T^m e^{\frac{-V_{G0}}{V_t}} \right] \right) A e^{\frac{V}{V_t}} & V > 0 \\ 0 & V < 0 \end{cases}$$

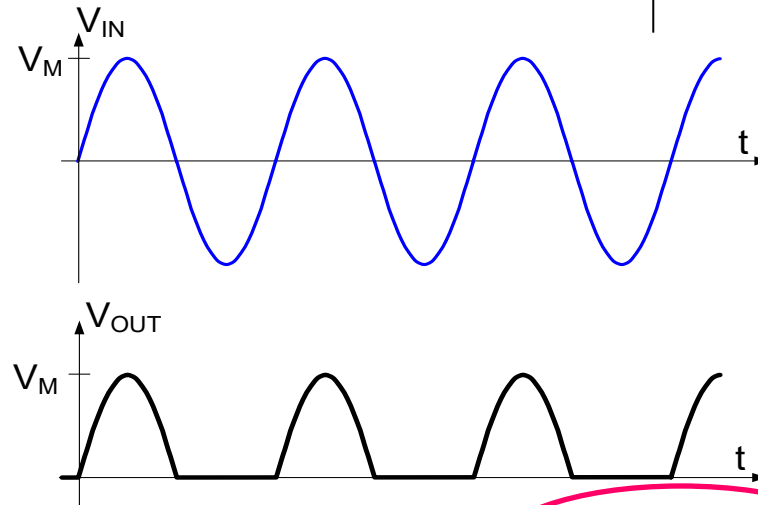
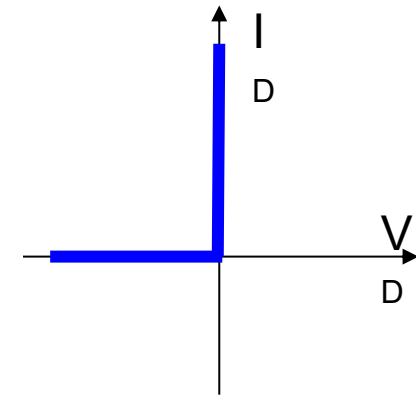
Typical values for key parameters:  $J_{sX}=0.5A/\mu^2$ ,  $V_{G0}=1.17V$ ,  $m=2.3$

Observe this simplification is a piecewise model !

# Rectifier Application:



Simple Diode Model:



Analysis based upon “passing current” in one direction and “blocking current” in the other direction

What principle was used in this analysis?

Was this analysis rigorous ?

Diode Equation (even simplification) unwieldy to work with analytically. **Why?**

World's simplest diode circuit

Determine  $V_{OUT}$

Assume forward bias, simplified diode equation model

$$5 = V_D + V_{OUT}$$

$$V_{OUT} = I_D \cdot 1K$$

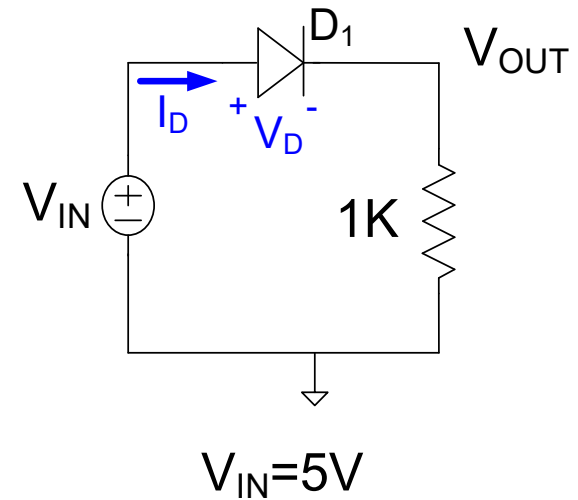
$$I_D = I_S e^{\frac{V_D}{nV_t}}$$

3 independent equations and 3 unknowns



$$V_{OUT} = I_S e^{\frac{5-V_{OUT}}{nV_t}} \cdot 1K$$

$$V_{OUT}=?$$



- Can obtain  $V_{OUT}$  from this equation but explicit expression does not exist for  $V_{OUT}$  !
- Previous analysis based upon “passing” and “blocking” currents was not rigorous !!

# I-V characteristics of pn junction

(signal or rectifier diode)

Diode Equation

$$I_D = I_S \left( e^{\frac{V_d}{nV_t}} - 1 \right)$$

$I_S$  often in the 10fA to 100fA range  
 $I_S$  proportional to junction area

$V_t$  is about 26mV at room temp

Simplification of Diode Equation:

$$I_D = \begin{cases} I_S e^{\frac{V_D}{nV_T}} & V > 0 \\ -I_S & V < 0 \end{cases}$$

How much error is introduced using the simplification for  $V_d > 0.5V$ ? (assume  $n=1$ )

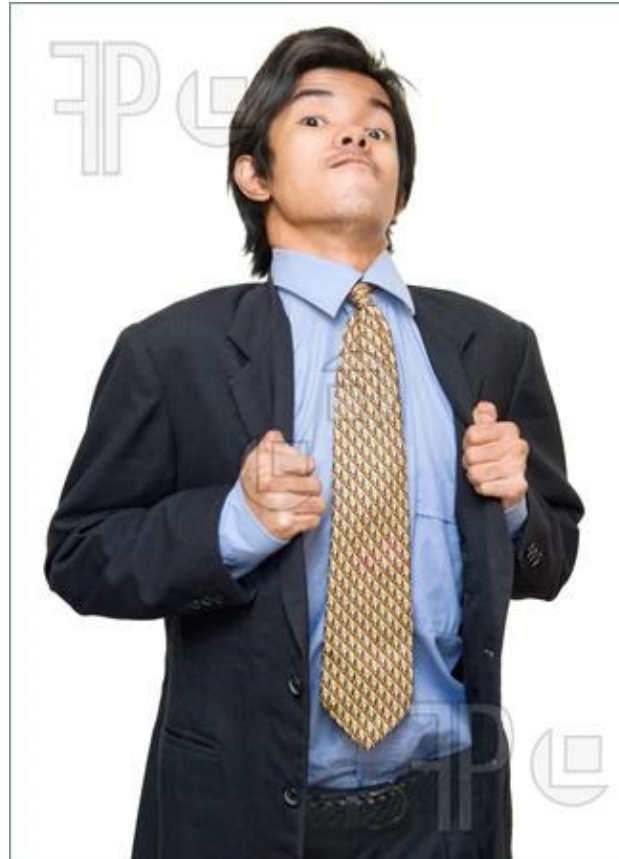
$$\varepsilon = \frac{I_S \left( e^{\frac{V_d}{V_t}} - 1 \right) - I_S e^{\frac{V_d}{V_t}}}{I_S \left( e^{\frac{V_d}{V_t}} - 1 \right)} \quad \varepsilon < \frac{1}{e^{\frac{0.5}{0.026}}} = 4.4 \bullet 10^{-9}$$

How much error is introduced using the simplification for  $V_d < -0.5V$ ?

$$\varepsilon < e^{\frac{-0.5}{0.026}} = 4.4 \bullet 10^{-9}$$

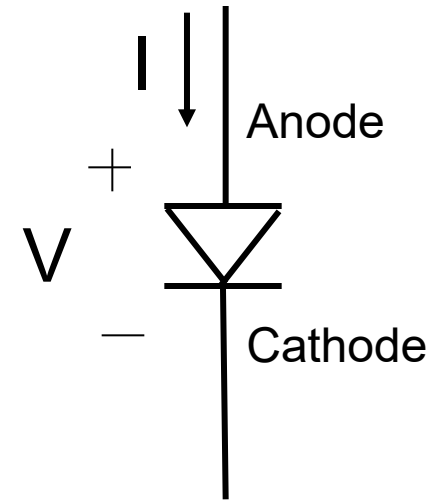
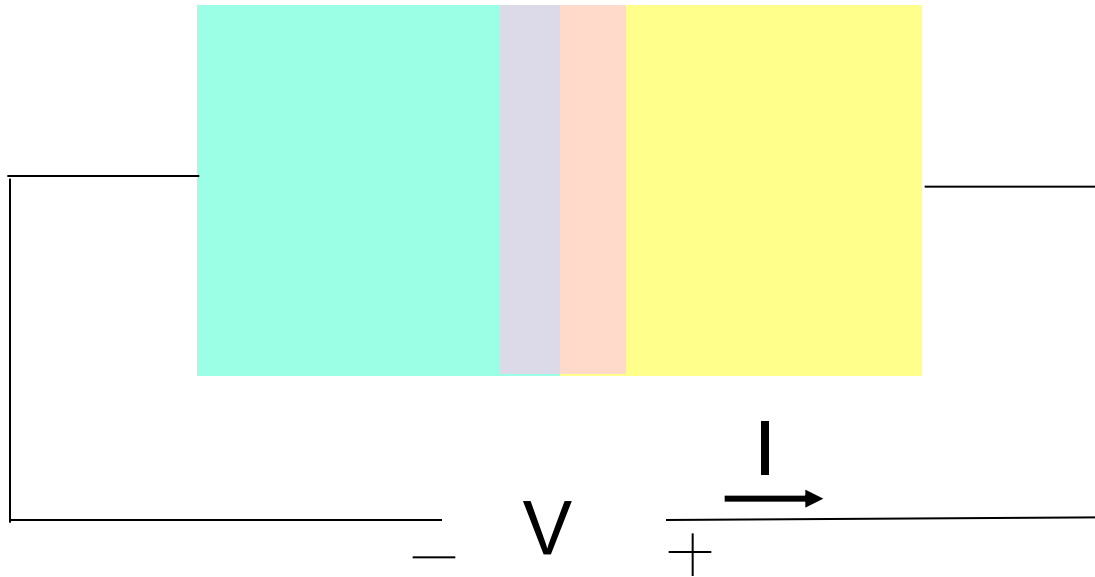
**Simplification almost never introduces any significant error**

Will you impress your colleagues or your boss if you use the more exact diode equation when  $V_d < -0.5V$  or  $V_d > +0.5V$  ?



Will your colleagues or your boss be unimpressed if you use the more exact diode equation when  $V_d < -0.5V$  or  $V_d > +0.5V$  ?

# pn Junctions



## “Diode Equation”:

(good enough for most applications  
when ideal diode model is inadequate)

$$I = \begin{cases} J_s A e^{\frac{v}{nV_T}} & V > 0 \\ 0 & V < 0 \end{cases}$$

Note:  $I_s = J_s A$

$J_s$  = Sat Current Density (in the 1aA/u<sup>2</sup> to 1fA/u<sup>2</sup> range)

A = Junction Cross Section Area

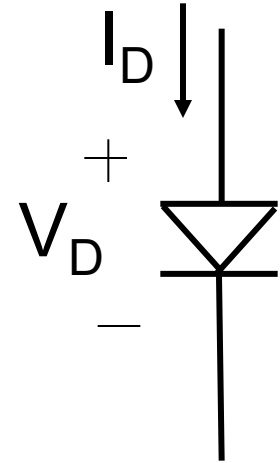
$V_T = kT/q$  (k/q = 1.381x10<sup>-23</sup>V•C/°K / 1.6x10<sup>-19</sup>C = 8.62x10<sup>-5</sup>V/°K)

n is approximately 1

# $I_S$ highly temperature dependent

Example: Consider diode operating under forward bias

$$I_D(T) = \left( J_{SX} \left[ T^m e^{\frac{-V_{G0}}{V_t}} \right] \right) A e^{\frac{V_D}{V_t}}$$



What percent change in  $I_S$  will occur for a  $1^\circ\text{C}$  change in temperature at room temperature?

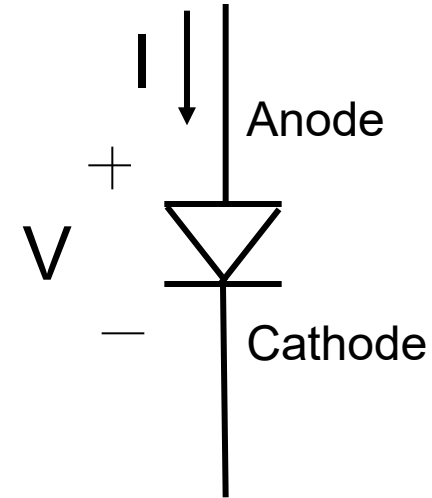
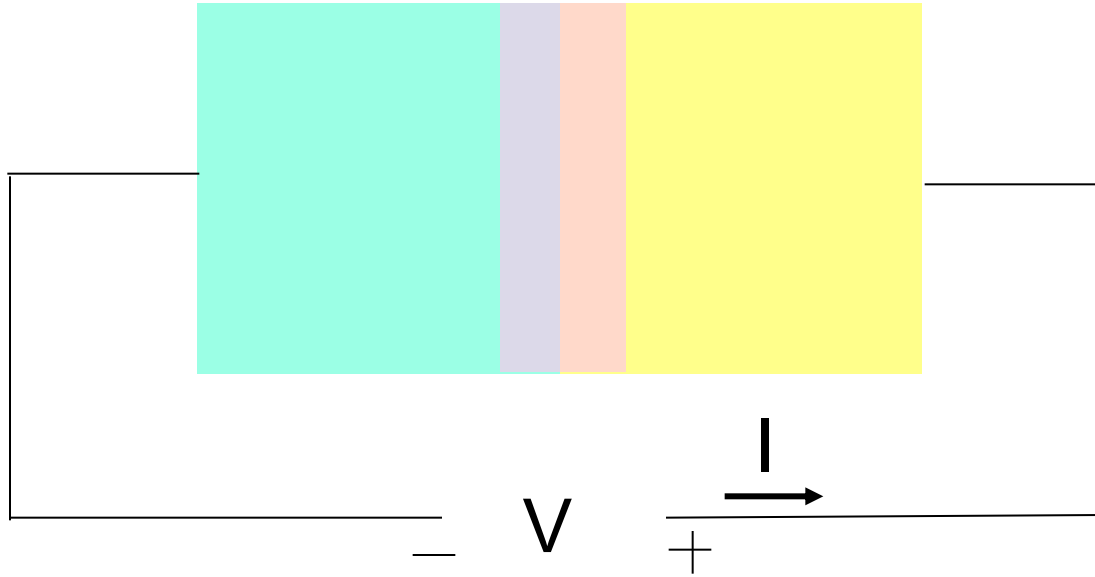
$$\frac{\Delta I_S}{I_S} = \frac{\left( J_{SX} \left[ T_{T_2}^m e^{\frac{-V_{G0}}{V_t(T_2)}} \right] \right) A - \left( J_{SX} \left[ T_{T_1}^m e^{\frac{-V_{G0}}{V_t(T_1)}} \right] \right) A}{\left( J_{SX} \left[ T_{T_1}^m e^{\frac{-V_{G0}}{V_t(T_1)}} \right] \right) A} = \frac{\left( \left[ T_{T_2}^m e^{\frac{-V_{G0}}{V_t(T_2)}} \right] \right) - \left( \left[ T_{T_1}^m e^{\frac{-V_{G0}}{V_t(T_1)}} \right] \right)}{\left( \left[ T_{T_1}^m e^{\frac{-V_{G0}}{V_t(T_1)}} \right] \right)}$$

$$\frac{\Delta I_S}{I_S} = \frac{(1.240 \times 10^{-15}) - (1.025 \times 10^{-15})}{(1.025 \times 10^{-15})} 100\% = 21\%$$

- Attempts to measure  $I_S$  in our laboratories can result in large errors !
- Most circuits whose performance depends upon precise value for  $I_S$  are not practical



# pn Junctions

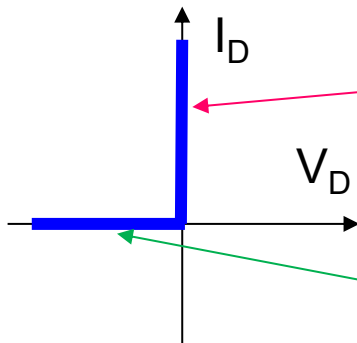


**Diode Equation:**  
(good enough for most applications)

$$I = \begin{cases} J_s A e^{\frac{v}{nV_T}} & V > 0 \\ 0 & V < 0 \end{cases}$$

$$I_s = J_s A$$

Simple Diode Model:

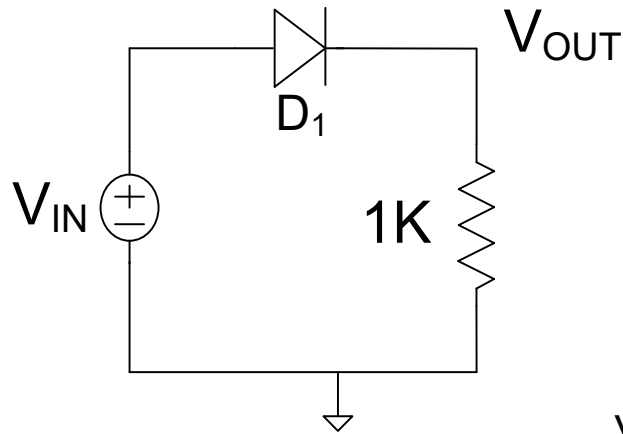


Often termed the “conducting” or “ON” state

Often termed the “nonconducting” or “OFF” state

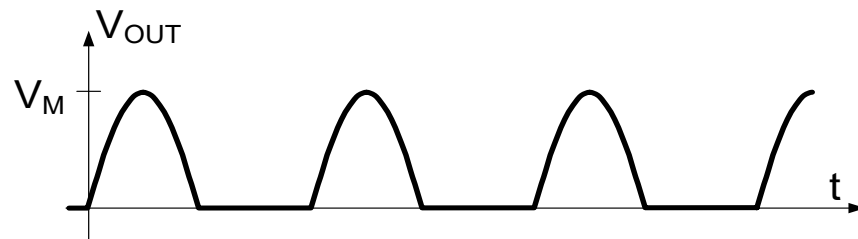
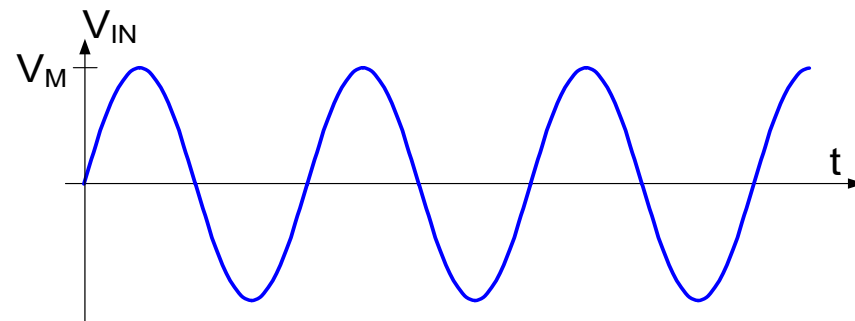
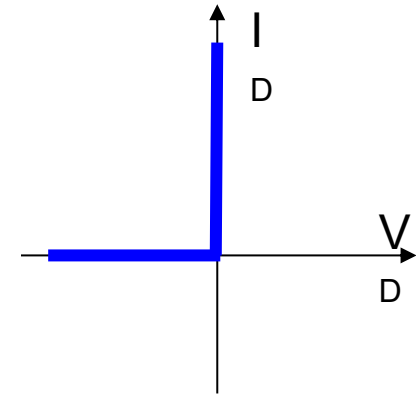
# What basic circuit analysis principles were used to analyze this circuit?

## Rectifier Application:



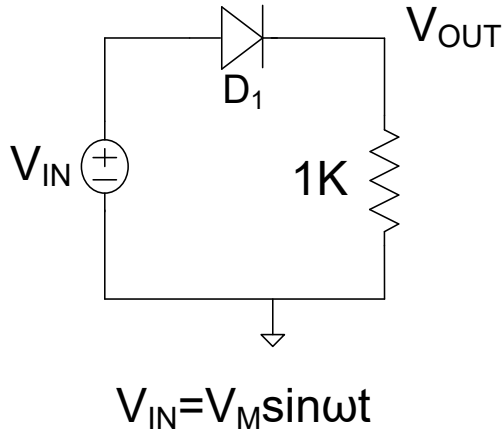
$$V_{IN} = V_M \sin \omega t$$

## Simple Diode Model:

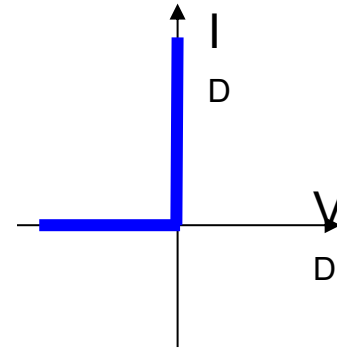


Analysis based upon “passing current” in one direction and “blocking current” in the other direction

# Rectifier Application:



## Simple Diode Model:

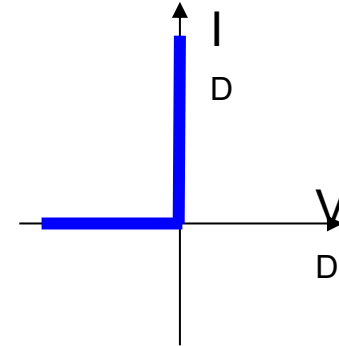
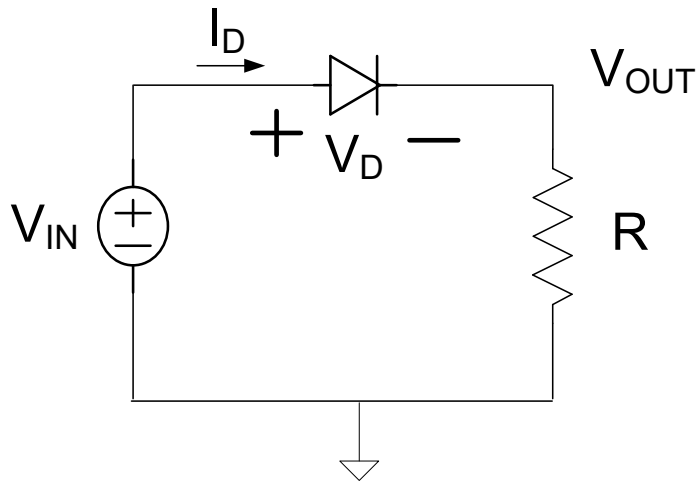


Analysis based upon “passing current” in one direction and “blocking current” in the other direction

**Was the previous analysis rigorous?**

**Is use of simple diode model justifiable?**

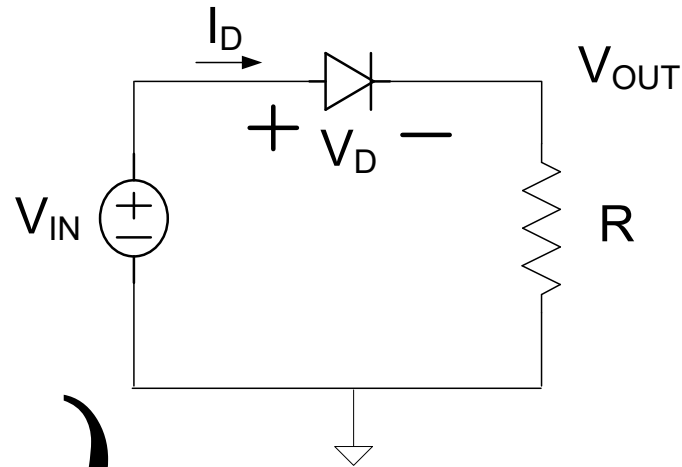
# Consider again the basic rectifier circuit



- Previously considered sinusoidal excitation
- Previously gave “qualitative” analysis
- **Rigorous analysis method is essential**

$$V_{\text{OUT}} = ?$$

# Consider again the basic rectifier circuit



$$V_{IN} = V_D + I_D R$$

$$V_{OUT} = I_D R$$

$$I_D = I_S \left( e^{\frac{V_D}{V_t}} - 1 \right)$$

$$V_{OUT} = I_S R \left( e^{\frac{V_{IN} - V_{OUT}}{V_t}} - 1 \right)$$

This analysis is rigorous (using only KVL and device models)

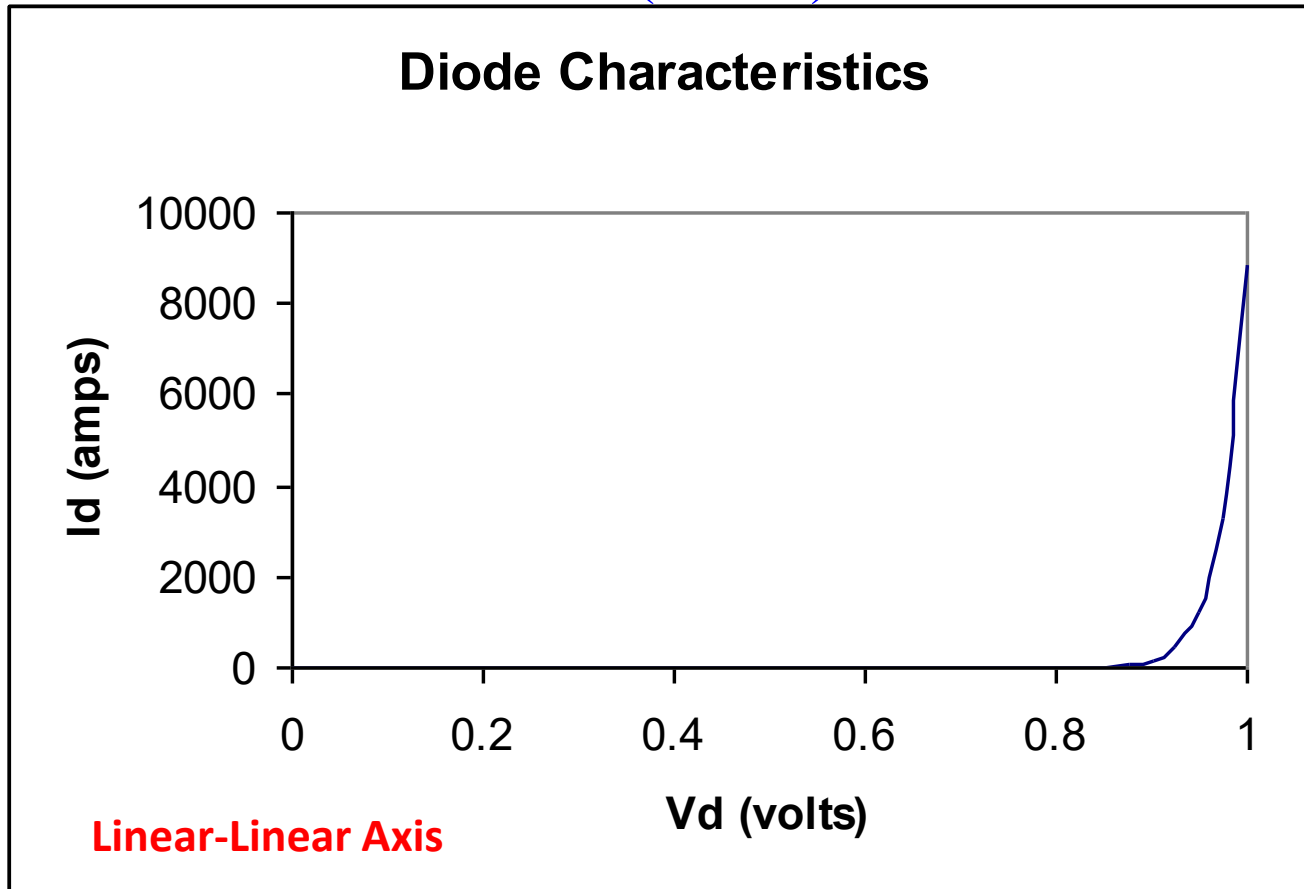
Even the simplest diode circuit does not have a closed-form explicit solution when diode equation is used to model the diode !!

Due to the nonlinear nature of the diode equation

**Simplifications of diode model are essential if analytical results are to be obtained !**

Lets study the diode equation a little further

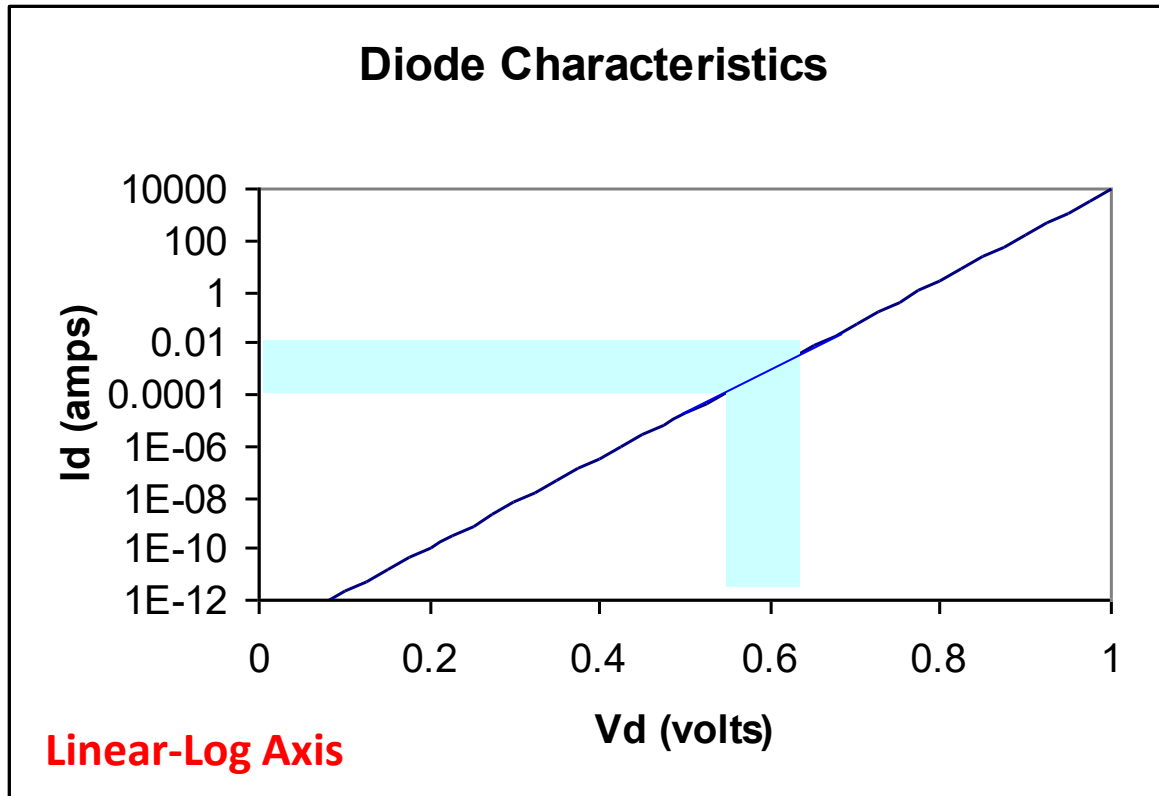
$$I_d = I_s \left( e^{\frac{V_d}{V_t}} - 1 \right)$$



Power Dissipation Becomes Destructive if  $V_d > 0.85V$  (actually less)

Lets study the diode equation a little further

$$I_d = I_s \left( e^{\frac{V_d}{V_t}} - 1 \right)$$

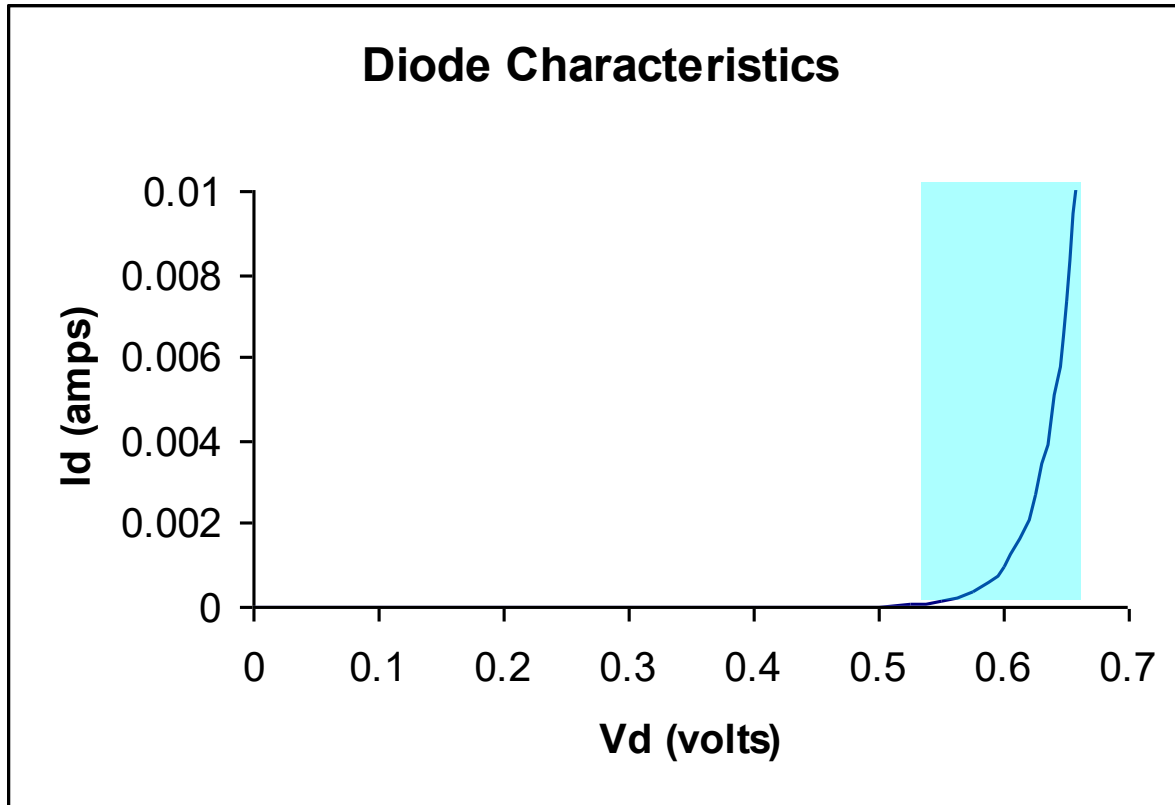


For two decades of current change, Vd is close to 0.6V

This is the most useful conducting current range for many applications

Lets study the diode equation a little further

$$I_d = I_s \left( e^{\frac{V_d}{V_t}} - 1 \right)$$



For two decades of current change,  $V_d$  is close to 0.6V

This is the most useful current range when conducting for many applications

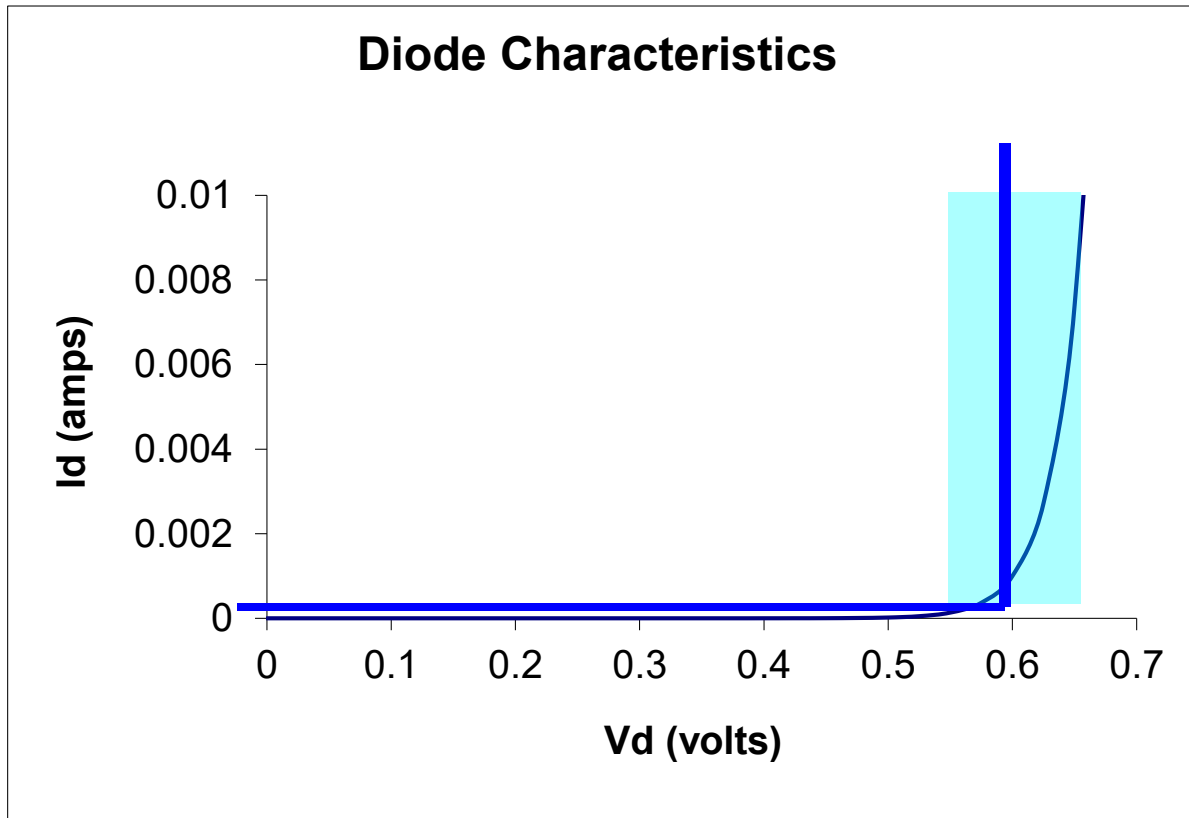


Lets study the diode equation a little further

$$I_d = I_s \left( e^{\frac{V_d}{V_t}} - 1 \right)$$



$$\begin{array}{ll} I_d = 0 & V_d < 0.6 \text{ V} \\ V_d = 0.6 \text{ V} & I_d > 0 \end{array}$$



Widely Used Piecewise Linear Model

# Which simplified model is better?

Both are about the same !

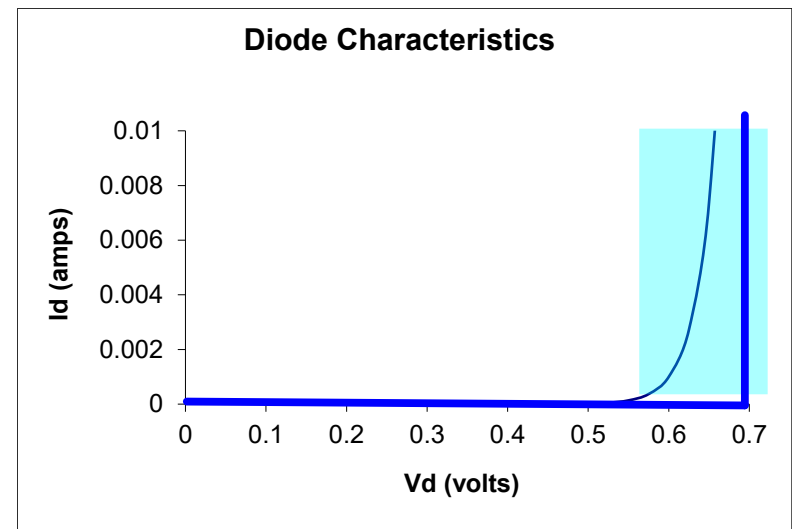
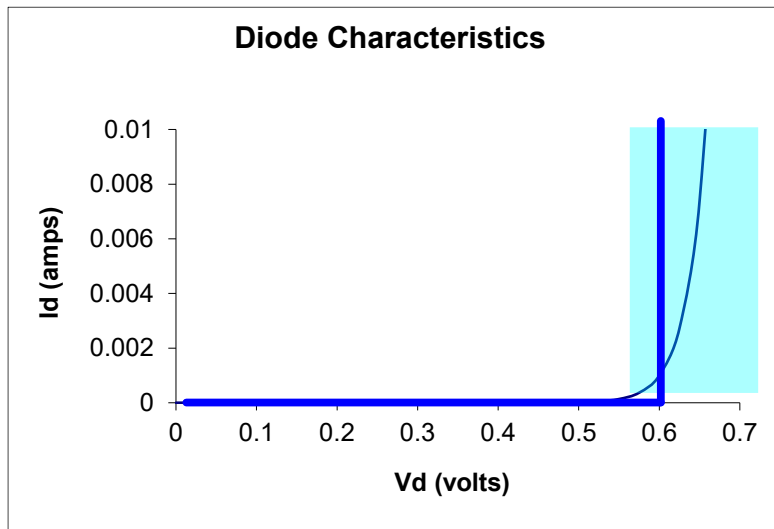
$$I_d = I_S \left( e^{\frac{V_d}{V_t}} - 1 \right)$$

$$I_d = 0 \quad V_d < 0.6 \text{ V}$$

$$V_d = 0.6 \text{ V} \quad I_d > 0$$

$$I_d = 0 \quad V_d < 0.7 \text{ V}$$

$$V_d = 0.7 \text{ V} \quad I_d > 0$$



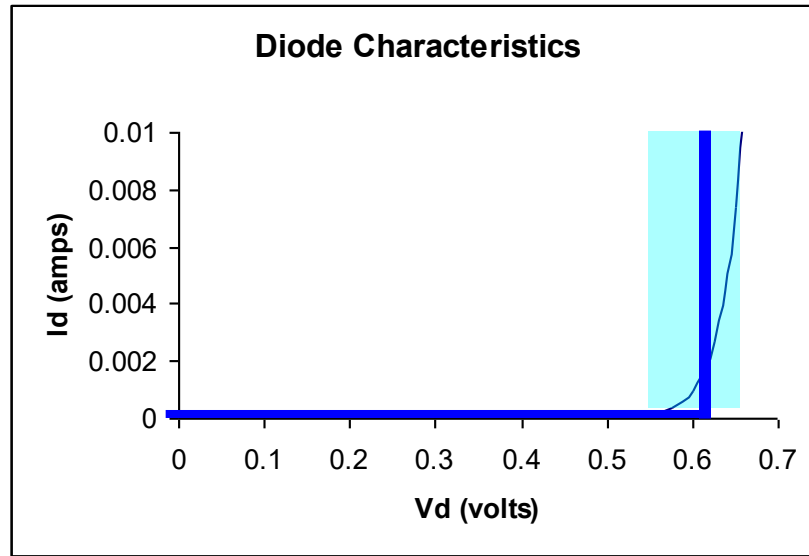
Widely Used Piecewise Linear Model

# Lets study the diode equation a little further

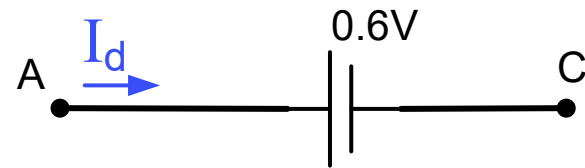
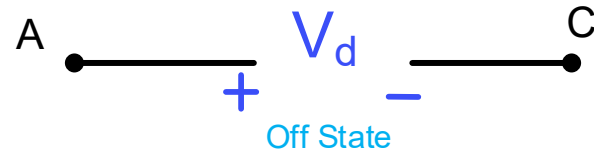
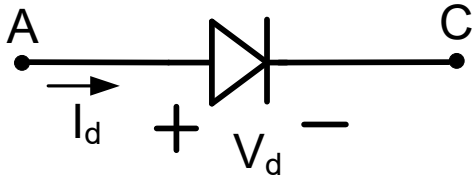
$$I_d = I_s \left( e^{\frac{V_d}{V_t}} - 1 \right)$$



$$\begin{aligned} I_d &= 0 & V_d < 0.6 \text{ V} \\ V_d &= 0.6 \text{ V} & I_d > 0 \end{aligned}$$

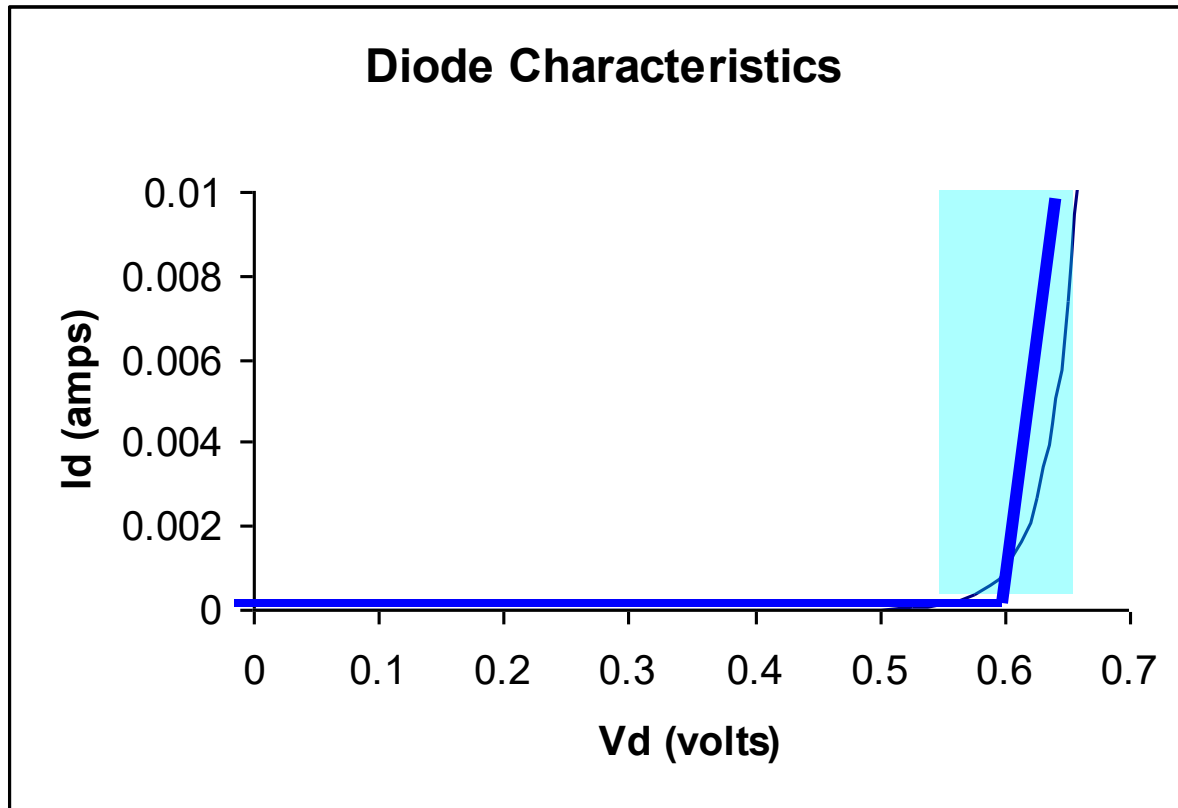


## Equivalent Circuit



Lets study the diode equation a little further

$$I_d = I_s \left( e^{\frac{V_d}{V_t}} - 1 \right)$$



Better model in "ON" state though often not needed

Includes Diode "ON" resistance

## Lets study the diode equation a little further

$$I_d = I_S \left( e^{\frac{V_d}{V_t}} - 1 \right)$$

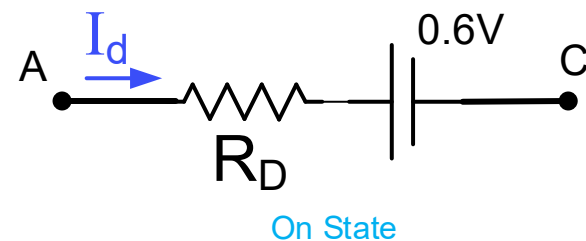
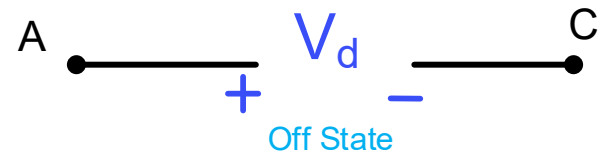
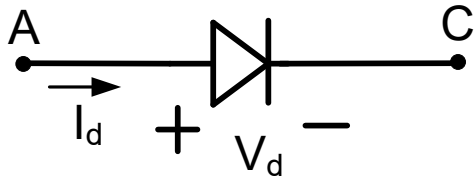
### Piecewise Linear Model with Diode Resistance

$$I_d = 0 \quad \text{if } V_d < 0.6V$$

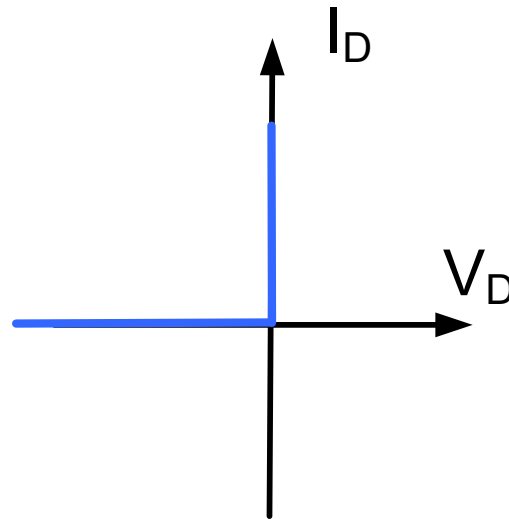
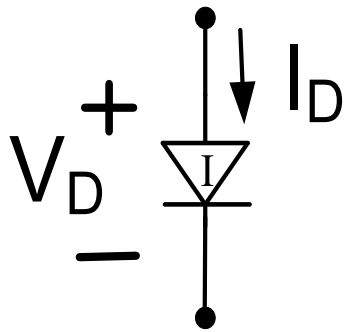
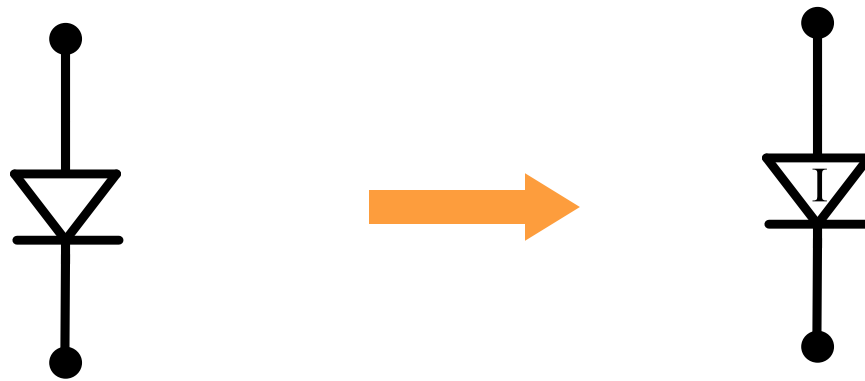
$$V_d = 0.6V + I_d R_D \quad \text{if } I_d > 0$$

( $R_D$  is rather small: often in the  $20\Omega$  to  $100\Omega$  range):

### Equivalent Circuit



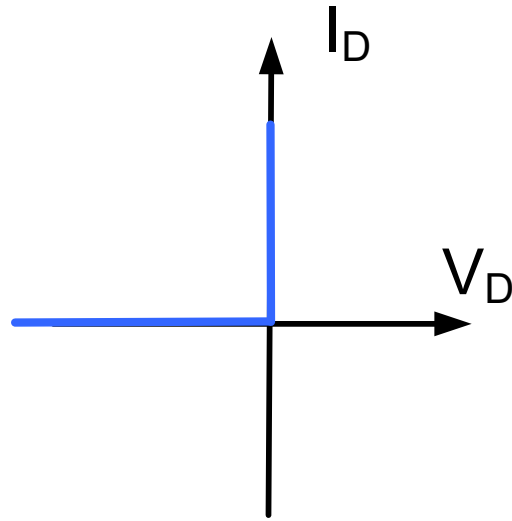
# The Ideal Diode



$$I_D = 0 \quad \text{if} \quad V_D \leq 0$$

$$V_D = 0 \quad \text{if} \quad I_D > 0$$

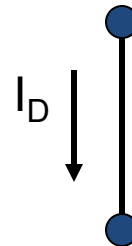
# The Ideal Diode



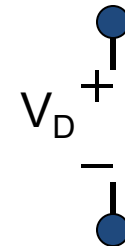
$$I_D = 0 \quad \text{if} \quad V_D \leq 0 \quad \text{“OFF”}$$
$$V_D = 0 \quad \text{if} \quad I_D > 0 \quad \text{“ON”}$$



“ON”



“OFF”



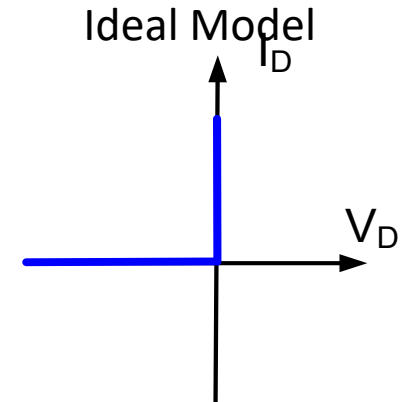
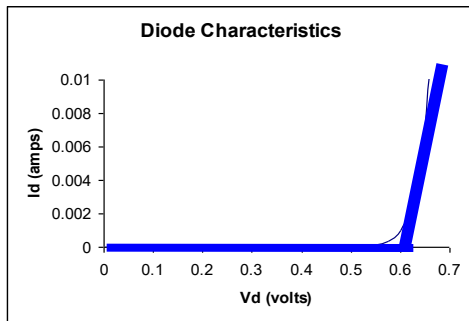
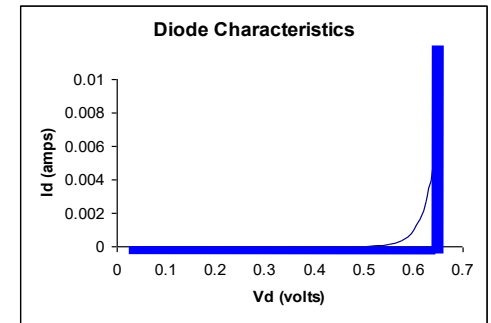
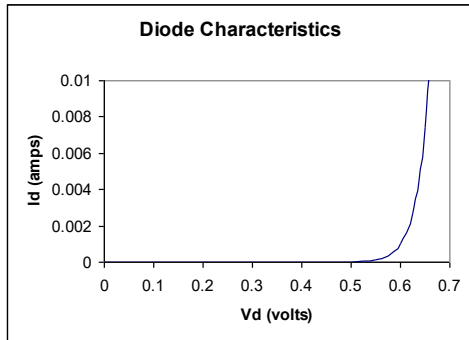
Valid for

$$I_D > 0$$

$$V_D \leq 0$$

# Diode Models

## Diode Equation (4 variants)



Which model should be used?

The simplest model that will give acceptable results in the analysis of a circuit

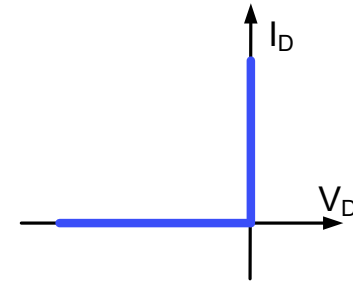


# Diode Model Summary

## Piecewise Linear Models

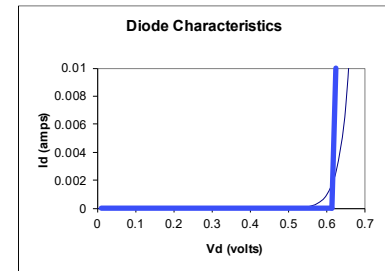
$$I_d = 0 \quad \text{if } V_d < 0$$

$$V_d = 0 \quad \text{if } I_d > 0$$



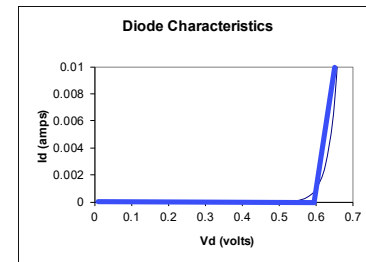
$$I_d = 0 \quad \text{if } V_d < 0.6V$$

$$V_d = 0.6V \quad \text{if } I_d > 0$$



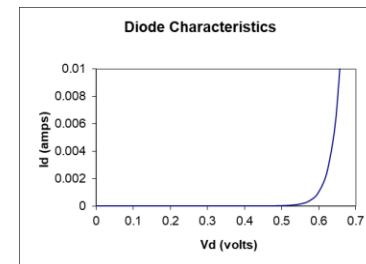
$$I_d = 0 \quad \text{if } V_d < 0.6$$

$$V_d = 0.6 + I_d R_d \quad \text{if } I_d > 0$$



## Diode Equation (or variants discussed)

$$I_d = I_s \left( e^{\frac{V_d}{V_t}} - 1 \right)$$



# Diode Model Summary

## Piecewise Linear Models

$$I_d = 0 \quad \text{if } V_d < 0$$

$$V_d = 0 \quad \text{if } I_d > 0$$

$$I_d = 0 \quad \text{if } V_d < 0.6V$$

$$V_d = 0.6V \quad \text{if } I_d > 0$$

$$I_d = 0 \quad \text{if } V_d < 0.6$$

$$V_d = 0.6 + I_d R_d \quad \text{if } I_d > 0$$

## Diode Equation (or variants discussed)

$$I_d = I_S \left( e^{\frac{V_d}{V_t}} - 1 \right)$$

When is the ideal model adequate?

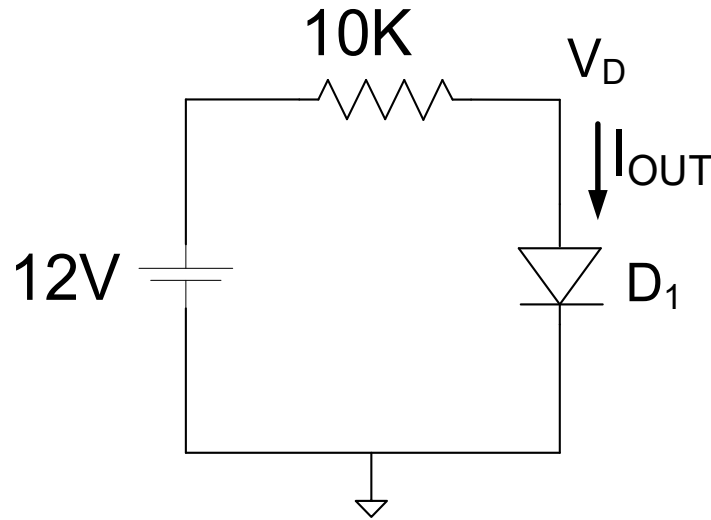
When it doesn't make much difference whether  $V_d = 0V$  or  $V_d = 0.6V$

When is the second piecewise-linear model adequate?

When it doesn't make much difference whether  $V_d = 0.6V$  or  $V_d = 0.7V$

Example:

Determine  $I_{OUT}$  for the following circuit



Solution:

If the diode equation model is used will obtain:

$$\left. \begin{aligned} 12 &= I_{OUT} \cdot 10K + V_D \\ I_{OUT} &= I_S \left( e^{\frac{V_D}{V_t}} - 1 \right) \end{aligned} \right\} \longrightarrow I_{OUT} = I_S \left( e^{\frac{-I_{OUT} \cdot 10K}{V_t}} e^{\frac{12}{V_t}} - 1 \right)$$

As in previous example, a closed-form explicit expression for  $I_{OUT}$  does not exist

Will now establish rigorous approach for solving this (and other) nonlinear circuit (with model uncertainty and piecewise models) with piecewise models and obtaining a practical solution !

# Devices in Semiconductor Processes

- Resistors
- Diodes
- Capacitors
- MOSFETs



Side Track!  
Analysis of Nonlinear Circuits

# Analysis of Nonlinear Circuits

(Circuits with one or more nonlinear devices)

What analysis tools or methods can be used?

KCL ?

Nodal Analysis ?

KVL?

Mesh Analysis ?

~~Superposition?~~

Two-Port Subcircuits ?

~~Voltage Divider ?~~

~~Passing Current ?~~

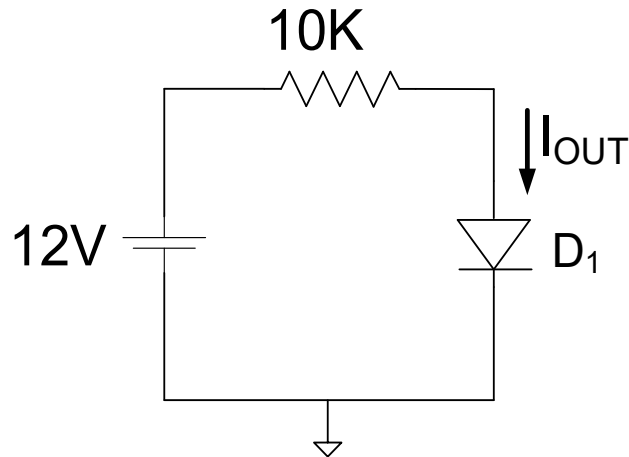
~~Current Divider?~~

~~Blocking Current ?~~

~~Thevenin and Norton Equivalent Circuits?~~

- How are piecewise models accommodated?
- Will address the issue of how to rigorously analyze nonlinear circuits with piecewise models later

Example: Determine  $I_{OUT}$  for the following circuit



$$I_{OUT} = I_S \left( e^{\frac{-I_{OUT} \cdot 10K}{V_t}} e^{\frac{12}{V_t}} - 1 \right)$$

- Results are accurate
- Analysis was tedious (and if slightly more complicated circuit even single implicit expression for output is often not attainable)
- Difficult to interpret results with implicit solution

Alternate Solution Strategy:

1. Assume PWL model with  $V_D=0.6V$ ,  $R_D=0$
2. Guess state of diode (ON)
3. Analyze circuit with model
4. Validate state of guess in step 2 (verify the “if” condition in model)

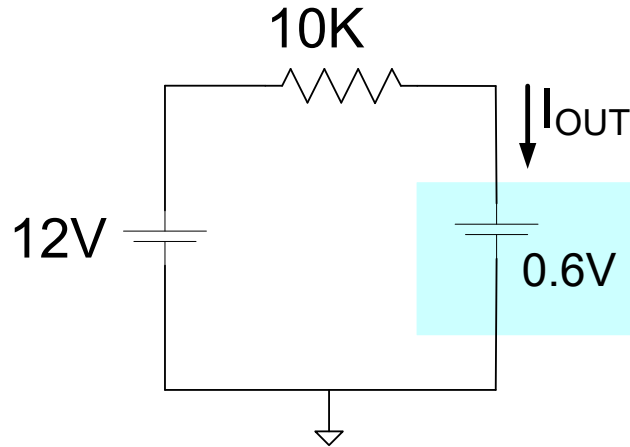
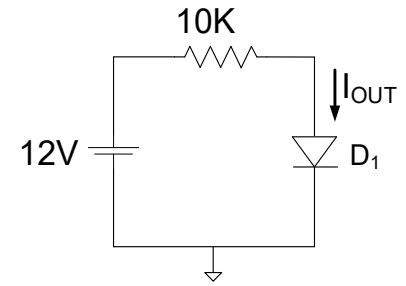
Select  
Model

5. Assume PWL with  $V_D=0.7V$
6. Guess state of diode (ON)
7. Analyze circuit with model
8. Validate state of guess in step 6 (verify the “if” condition in model)
9. Show difference between results using these two models is small
10. If difference is not small, must use a different model

Validate  
Model

## Alternate Solution:

1. Assume PWL model with  $V_D=0.6V$ ,  $R_D=0$ ,  $I_S=10FA$
2. Guess state of diode (ON)



3. Analyze circuit with model

$$I_{OUT} = \frac{12V - 0.6V}{10K} = 1.14mA$$

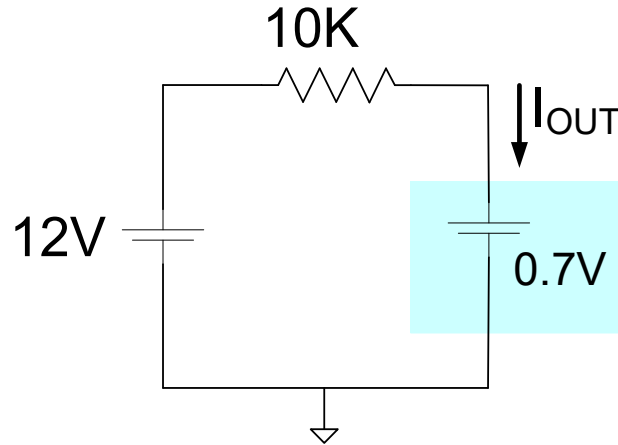
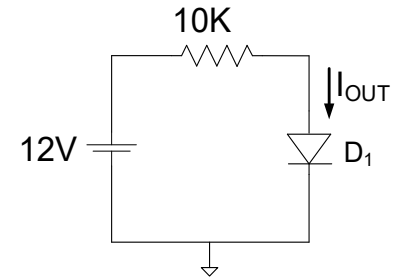
4. Validate state of guess in step 2

To validate state, must show  $I_D > 0$

$$I_D = I_{OUT} = 1.14mA > 0$$

## Alternate Solution:

5. Assume PWL model with  $V_D=0.7V$ ,  $R_D=0$ ,  $I_S=10FA$
6. Guess state of diode (ON)



7. Analyze circuit with model

$$I_{OUT} = \frac{12V - 0.7V}{10K} = 1.13mA$$

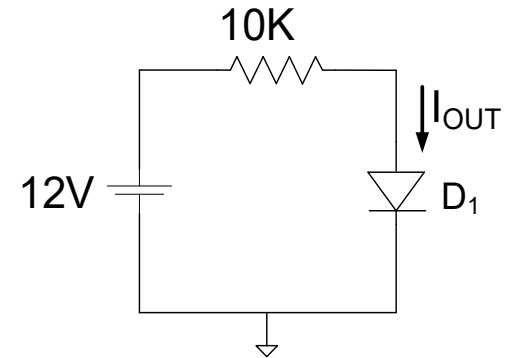
8. Validate state of guess in step 6

To validate state, must show  $I_D > 0$

$$I_D = I_{OUT} = 1.13mA > 0$$



Alternate Solution:



9. Show difference between results using these two models is small

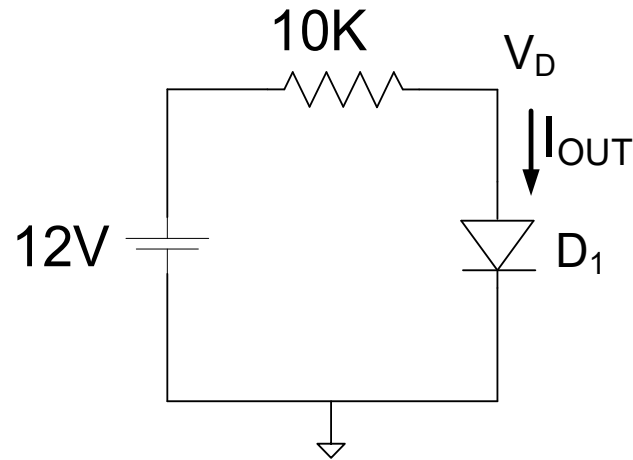
$I_{\text{OUT}} = 1.14\text{mA}$  and  $I_{\text{OUT}} = 1.13\text{ mA}$  are close

Thus, can conclude

$$I_{\text{OUT}} \cong 1.14\text{mA}$$

Example:

Determine  $I_{OUT}$  for the following circuit



How do the two solutions compare?

With diode equation model for  $I_S=10\text{fA}$  :

$$I_{OUT} = I_S \left( e^{\frac{-I_{OUT} \cdot 10K}{V_t}} e^{\frac{12}{V_t}} - 1 \right) \Rightarrow I_{OUT} = 1.134\text{mA}$$

With PWL model:

$$I_{OUT} \cong 1.14\text{mA}$$

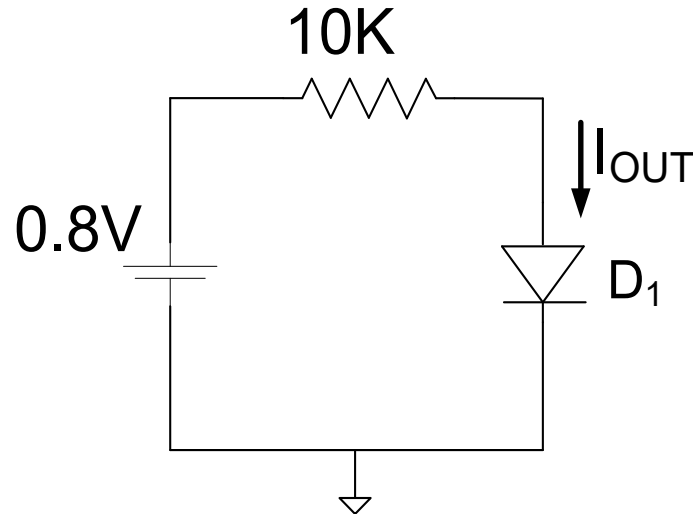
What was the major reason the PWL model simplified the analysis?

Piecewise Linear Model

Example:

Determine  $I_{OUT}$  for the following circuit

Supply Changed  
from 12V to 0.8V



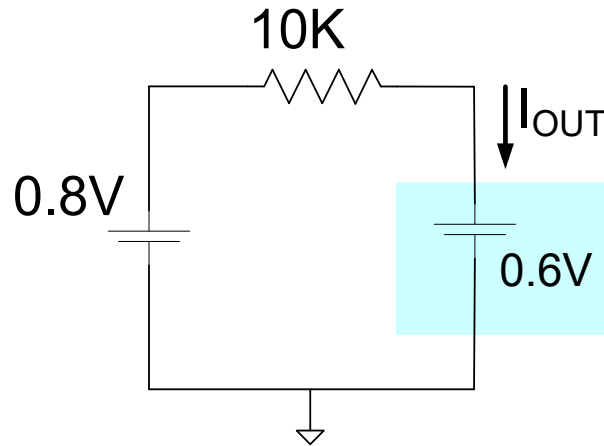
Solution:

Strategy:

1. Assume PWL model with  $V_D=0.6V$ ,  $R_D=0$
2. Guess state of diode (ON)
3. Analyze circuit with model
4. Validate state of guess in step 2
5. Assume PWL with  $V_D=0.7V$
6. Guess state of diode (ON)
7. Analyze circuit with model
8. Validate state of guess in step 6
9. Show difference between results using these two models is small
10. If difference is not small, must use a different model

Solution:

1. Assume PWL model with  $V_D=0.6V$ ,  $R_D=0$
2. Guess state of diode (ON)



3. Analyze circuit with model

$$I_{OUT} = \frac{0.8 - 0.6V}{10K} = 20\mu A$$

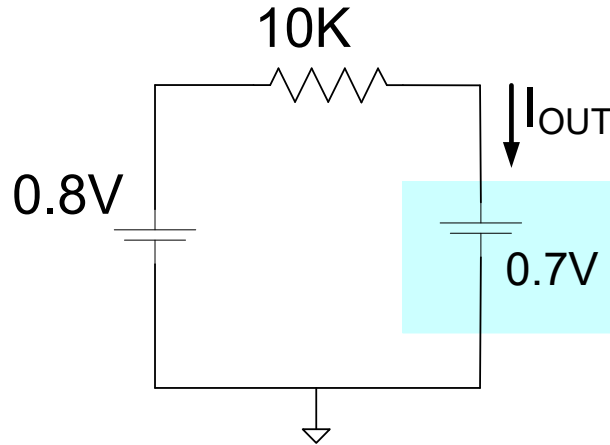
4. Validate state of guess in step 2

To validate state, must show  $I_D > 0$

$$I_D = I_{OUT} = 20\mu A > 0$$

Solution:

5. Assume PWL model with  $V_D=0.7V$ ,  $R_D=0$
6. Guess state of diode (ON)



7. Analyze circuit with model

$$I_{OUT} = \frac{0.8V - 0.7V}{10K} = 10\mu A$$

8. Validate state of guess in step 6

To validate state, must show  $I_D > 0$

$$I_D = I_{OUT} = 10\mu A > 0$$

Solution:

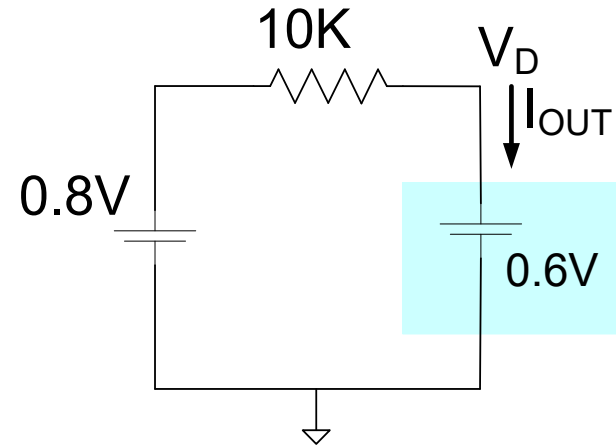
9. Show difference between results using these two models is small

$$I_{\text{OUT}} = 10\mu\text{A} \text{ and } I_{\text{OUT}} = 20\mu\text{A} \quad \text{are not close}$$

10. If difference is not small, must use a different model

Thus must use diode equation to model the device

$$I_{\text{OUT}} = \frac{0.8 - V_D}{10\text{K}}$$
$$I_{\text{OUT}} = I_S e^{\frac{V_D}{V_t}}$$



Solve simultaneously, assume  $V_t = 25\text{mV}$ ,  $I_S = 1\text{fA}$

Solving these two equations by iteration, obtain  $V_D = 0.6148\text{V}$  and  $I_{\text{OUT}} = 18.60\mu\text{A}$

# Use of Piecewise Models for Nonlinear Devices when Analyzing Electronic Circuits

## Process:

1. Guess state of the device
2. Analyze circuit
3. Verify State
4. Repeat steps 1 to 3 if verification fails
5. Verify model (if necessary)

## Observations:

- Analysis generally simplified dramatically (particularly if piecewise model is linear)
- Approach applicable to wide variety of nonlinear devices
- Usually much faster than solving the nonlinear circuit directly
- Wrong guesses in the state of the device do not compromise solution (verification will fail)
- Helps to guess right the first time
- Detailed model is often not necessary with most nonlinear devices
- Particularly useful if piecewise model is PWL (but not necessary)
- Closed-form solutions (attainable with PWL models) give insight into performance of circuit
- For practical circuits, the simplified approach with piecewise models usually applies

**Key Concept For Analyzing Circuits with Nonlinear Devices**



Stay Safe and Stay Healthy !



End of Lecture 15